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Based on: NATIONAL INSTITUTE OF OPEN SCHOOLING – X

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Solved Sample Paper - 1

Based on NIOS (National Institute of Open Schooling)

Mathematics - X

Time :	3 Ho	urs]	[]	Maximum Marks : 100
Note:	(i)	Question Numbers (1-14) are Multiple each question, four alternative choice have to select the correct alternative a (D) as the case may be.	e Choice Questions. Each questic es A, B, C, D are given, of which and indicate it in the answer-book	on carries one mark. For only one is correct. You by writing (A), (B), (C) or
	(ii)	Question Numbers (15-24) carry 2 ma	arks each.	
	(iii)	Question Numbers (25-33) carry 5 ma	arks each.	
	(iv)	Question Numbers (34-36) carry 7 ma	arks each	
	(V)	All questions are compulsory.		
			(c) 5	(d) 25
Q. 1.	0.062	25 can be written in the form $\frac{p}{2}$ as:	Ans. (c) 5.	(0) 20
		$q \simeq$	Q. 7. ÁBCD is a cyclic	c quadrilateral in which
	1		\angle BCD = 100° and \angle ABD = 7	70º. The ∠ADB is:
(a)	8	<i>(0)</i> 8	(a) 100°	(b) 70°
	5	1	$(c) 30^{\circ}$	(d) 15°
(C)	16	(d) <u>+</u>	Q. 8. If 5 tan A =	4. than the value of
	10			
Ans.	(b) -		$\frac{5 \sin A - 4 \cos A}{1 + 1 + 1 + 1 + 1}$ is:	
0.0	16 vr -	1 is a zero of the network Γ (γ) =	5 sin A + 4 cos A	
Q. 2. v ² – 5v +	If $X = k$ the	= 1 is a zero of the polynomial F (x) =	aihooks	C. (5 m)
∧ − 5x − (a)	4	(b) = 4		(b) — 6
(a) (c)	6	$(\vec{a}) - \vec{6}$	-	-
Ans.	(a) 4.	 -	(c) —	(d) 0
Q. 3.	5 gm	is what per cent of a kilograme?	Ans. (d) 0.	
(a)	10	(b) 5 (c) 0.05	Q. 9. If tan ² 45° – cos ²	30° = x sin 45°. cos 45°,
Ans.	(c) 0	(<i>u</i>) 0.05	then the value of <i>x</i> is:	
Q. 4.	Mark	ed price of a shirt is Rs. 500. A cus-		<u> </u>
tomer bu	ys the	e shirt for Rs. 400, the rate of discount	(a) –2	(b) - <u>-</u> 2
is:		<i>"</i>	1	-
(a)	20%	(b) 22%	(c) <u>-</u>	(d) 2
(C) Δns	23%	(<i>a)</i> 30%	2	
Q. 5.	In a	triangle, the point of intersection of	Ans $(c) = \frac{1}{c}$	
perpendi	icular	bisectors is called:	2	
(a)	Ince	ntre (b) Orthocentre	Q. 10. The value of cos	ec ² 67° – tan ² 23° + 1 is:
(C)	Circu	umcentre (d) Centroid	(a) –1	(b) 0
Ans.		ircumcentre.	(c) 1	(d) 2
a circle,	of rac	dius 3 cm, is 4 cm. The distance (in	O Ans. (<i>a</i>) 2. O 11 The value of (sin	$(2 \Delta - 1) \cos^2(90^\circ - \Delta)$
cm) of A	from	the centre of the circle is:	is:	A)
(a)	./7	<i>(b)</i> 7	<i>(a)</i> –1	<i>(b)</i> 0
(u)	$\sqrt{1}$			

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(c) 1

Ans. (c) 1.

Q. 12. If the arithmetic mean of 5, 8, 6, 7, x and 4 is 6, then the value of x is:

(d) $\sqrt{2}$

- (a) 4 (b) 6 (d) 12
- (c) 1
- Ans. (b) 6.

Q. 13. The median of first six prime numbers is: (a) 7 (b) 6 (d) 4.6

- (c) 5
- Ans. (b) 6.

Q. 14. In the bar graph given below, which game is played by the maximum number of students?



Q. 17. By selling a shirt to a customer for Rs. 360 a shopkeeper makes a profit of 20%. For how much should he sell it to make a profit of 30%?

Ans. Price =
$$360 \times \frac{130}{100}$$

Q. 18. Find the centroid of a triangle ABC whose vertices are A (3, - 1), B (10, 7) and Č (5, 3). Ans. Co-ordinates of the centroid

$$= \left(\frac{x_1 + x_2 + x_3}{3}, \frac{y_1 + y_2 + y_3}{3}\right)$$
$$= \left(\frac{3 + 10 + 5}{3}, \frac{-1 + 7 + 3}{3}\right)$$
$$= (6, 3)$$

Q. 19. Two adjacent angles of a rhombus are in the ratio 4:5. Find all the angles of the rhombus. Ans. Let the rhombus be ABCD and the common multiple be x











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MODULE-1

Number Systems

SUMMARY

When a child starts saying, "I will eat a chapati", he has started using his knowledge of numbers. Man is always curious by nature. He is always questioning "How?" This born eagerness was the starting of the number systems.

Natural Numbers: The numbers 1, 2, 3, used for counting the objects are called *Natural Numbers*.

Whole Numbers: If 0 is added to natural numbers, the system is known as *Whole Numbers*, i.e. 0, 1, 2, 3,

Integers: -4, -3, -2, -1, 0, 1, 2, 3, 4 are known as *Integers*.

 \dots -4, -3, -2, -1 are known as *Negative Integers* and 1, 2, 3, 4....are known as *Positive Integers*.

Even Numbers: The numbers which are divisible by 2 are known as *Even Numbers* e.g. 2, 4, 6, 8

Odd Numbers: The numbers which are not divisible by 2 are called *Odd Numbers*, e.g. 1, 3, 5, 7

Prime Numbers: The numbers which have no factors other than one and the numbers themselves are called the *Prime Numbers*, e.g. 2, 3, 5, 7, 11, 13

Note: Remember 1 is not a Prime Number.

Rational Numbers: A number of the form $\frac{p}{q}$, where

p and q are integers and $q \neq 0$ is called a *Rational Number*. p is called *numerator* and q is called *denominator*.

Irrational Numbers: All the real numbers which are not rational numbers are known as *irrational numbers*,

e.g. $\sqrt{2}$, .3121231234



ALGEBRA

Operations on Rational Numbers: For two positive rational numbers, the result after operation is a positive rational number. This law is known as *Closure Property*.

The result is unchanged even after the places of the numbers are interchanged. This law is known as *Cummutative Property*, e.g.

a+b=b+a Or ab=ba.

For Three Numbers: If the order of operation is changed, there is no change in result. This is called *Associative Property*, e.g.

(a + b) + c = (a + (b + c) Or a (bc) = (ab) c.

Positive and Negative Rational Numbers: If numerator and denominator of a rational number are positive or negative, it is called *Positive Rational Number* and if either numerator or denominator is negative, it is called a *Negative Rational Number*.

The Lowest Form of a Rational Number: The

rational number $\frac{a}{b}$ is said to be in its lowest form or

simplest form, if a and b have no common factors other than one.

Highest Common Factor (H.C.F.): The largest number by which the given numbers are fully divided is known as H.C.F. of the numbers.

Lowest Common Multiplication (L.C.M.): The smallest number which is divisible by the given numbers is known as L.C.M. of the numbers.

Example: Find the H.C.F. and L.C.M. of 24 and 30.

Sol. (*i*) The H.C.F.
$$24 = 2 \times 2 \times 2 \times 3$$

 $30 = 2 \times 3 \times 5$

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The H.C.F. of 24 and 30 is $2 \times 3 = 6$ Second Method: $24\overline{)30(1)}$ $\underline{24}$ 6) 24 (4)

Hence, H.C.F. is 6. (ii) The L.C.M. of 24 and 30. $24 = 2 \times 2 \times 2 \times 3$ $30 = 2 \times 3 \times 5$

L.C.M. of 24 and 30 is $2 \times 2 \times 2 \times 3 \times 5 = 120$ • Formula:

H.C.F. × L.C.M. = First Number × Second Number. Operations on Rational Numbers

Addition: The addition of positive numbers is positive and of negative numbers is negative.

If zero (0) is added to any number the sum is equal to that number.

a + 0 = a

If $\frac{a}{b}$ is a rational number, the rational number

 $-\frac{a}{b}$ is called the *negative* or *opposite* of $\frac{a}{b}$, because $\frac{a}{b} + \left(\frac{-a}{b}\right) = 0$

Subtraction: To subtract one rational number from another rational number, add the *negative* of the first rational number to the second rational number.

Multiplication: To multiply two rational numbers we multiply the numerators of both the numbers to get the numerator of the product and denominators of both the numbers to get the denominator of the product.

 $\frac{a}{b} \times \frac{c}{d} = \frac{ac}{bd}$

where a, b, c and d are integers and $b, d \neq 0$

 $1 \times a = a$ for every rational number a, $-1 \times a = -a$ the opposite of every rational number a.

The rational number $\frac{b}{a}$ is the reciprocal of the

rational number $\frac{a}{b}$, if $a \neq 0$, because $\frac{a}{b} \times \frac{b}{a} = 1$.

Division: To divide a rational number by a non-zero rational number, we multiply the first rational number by the reciprocal of the second number.

Division by zero (0) is not defined.

Number Line: The real numbers can be represented on a line is called the *Number Line*.

A line is drawn and zero (0) point is made in the middle. The negative points are taken on left side of zero, while positive points are taken on right side of the zero.

Decimal Representation of Rational Numbers: All the rational numbers can be represented in the decimal form.

Real Numbers: Rational numbers with irrational numbers form the system of real numbers.

Approximation of Irrational Numbers: The process of counting a decimal upto a specific number of places is called *rounding off.*

Method: To round off a decimal upto three places, we look at the digit in the fourth place and

(i) If this digit is less than 5, we ignore it and all digits after it, and write the remaining number i.e. the number upto 3 decimal places.

(ii) If the digit is 5 or more than 5, we add one to the digit in the third place and write the new number upto the three decimal places.

CHECK YOUR PROGRESS 1.1

Q. 1. Identify rational numbers and integers from the following:

$$4, \frac{-3}{4}, \frac{5}{6}, -36, \frac{12}{7}, \frac{3}{-8}, \frac{15}{7}, -$$

Sol. Integers 4, -36, -6

Rational numbers

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$$,\frac{-3}{4},\frac{5}{6},-36,\frac{12}{7},\frac{-3}{8},\frac{15}{7},-6$$

- Q. 2. From the following identify those which are not:
 - (i) natural numbers

$$-\frac{7}{4}, 16, \frac{-3}{7}, -15, 0, \frac{5}{17}, \frac{3}{-4}, -\frac{4}{3}$$

Sol. (i) Following are not natural numbers:

$$\frac{-7}{14}, \frac{-3}{7}, 15, 0, 0, \frac{5}{17}, \frac{-3}{4}, \frac{-3}{17}, \frac{-3}{4}, \frac{-3}{17}, \frac{-$$

- (*ii*) whole numbers
- Sol. Following are not natural numbers:

$$\frac{-7}{14}, \frac{-3}{7}, -15, \frac{5}{17}, \frac{-3}{4}, \frac{-4}{3}$$

- (iii) integers
- Sol. Following are not integers:

$$\frac{-7}{14}, \frac{-3}{7}, \frac{5}{17}, \frac{-3}{4}, \frac{-4}{3}$$

- *(iv)* rational numbers
- Sol. All are rational numbers.
- Q. 3. By making the following rational numbers with same denominator, simplify the following and specify whether the result in each case is a natural number, whole number, integer or a rational number:

NUMBER SYSTEMS / 3

(i)
$$3 + \frac{7}{3}$$

(i) $3 + \frac{7}{3} = \frac{3}{3} + \frac{7}{3} = \frac{3 \times 3 + 7}{3} = \frac{9 + 7}{3}$
(j) $\frac{12 - 12}{2} = 0$, whole number, integer and rational number.
Sol. $3 + \frac{7}{3} = \frac{3}{3} + \frac{7}{3} = \frac{3 \times 3 + 7}{3} = \frac{9 + 7}{3}$
(j) $\frac{9}{2} - \frac{1}{2}$
(j) $\frac{9}{2} - \frac{1}{2} = \frac{9 - 1}{2} = \frac{8}{2} = 4$, All.
(ii) $-3 + \frac{10}{4}$
(iii) $-3 + \frac{10}{4} = \frac{-3 \times 4 + 10}{4} = \frac{-12 + 10}{4} = \frac{-2}{4}$
Sol. $-3 + \frac{10}{4} = \frac{-3 \times 4 + 10}{4} = \frac{-12 + 10}{4} = \frac{-2}{4}$
Sol. $2 \times \frac{5}{7} = \frac{10}{7}$, rational number.
(iii) $8 + 3$
Sol. $-8 - 13 = -21$, integer and rational number.
(iii) $-9 + (-7)$
(iii) $(-5) + (-3)$
(iii) $(-5) + (-3) = \frac{10}{7} + \frac{10}{7} + \frac{10}{5} + \frac{10}{4} + \frac{10}{3} + \frac{10}{2} + \frac{10}{2} + \frac{10}{3} + \frac{10}{2} + \frac{10}{3} + \frac{10}{5} + \frac{10}{7} + \frac{10}{8} + \frac{10}{1} + \frac{10}{1}$

$$\frac{3}{7}, \frac{-6}{7}$$

Q. 6. Which of the following rational numbers are integers?

$$-10, \frac{15}{5}, \frac{-5}{15}, \frac{13}{5}, \frac{27}{9}, \frac{7 \times 3}{14}, \frac{-6}{-2}$$

(*i*)
$$\frac{2}{5}$$

 $\frac{-6}{-2} = \frac{-3 \times 2}{-2} = 3$

rational numbers:

Q. 7. Write 3 rational numbers equivalent to given

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Sol.
$$\frac{2}{5} = \frac{2 \times 2}{5 \times 2} = \frac{4}{10}$$
 (i) $\frac{3}{4}$
 $\frac{2}{5} = \frac{2 \times 3}{5 \times 3} = \frac{6}{15}$ Sol. $\frac{3}{4}$
 $\frac{2}{5} = \frac{2 \times 4}{5 \times 4} = \frac{8}{20}$
 $\frac{2}{5} = \frac{4}{10} = \frac{6}{15} = \frac{8}{10}$ $0 < \frac{3}{4} < 1; divide 4 equal parts of 1; i.e. A is 3/4.$
(ii) $\frac{-5}{6} = \frac{-5 \times 2}{6 \times 2} = \frac{-10}{12}$ Sol. $\frac{1}{2}$
 $\frac{-5}{6} = \frac{-5 \times 2}{6 \times 2} = \frac{-10}{12}$ Sol. $\frac{1}{2}$
 $\frac{-5}{6} = \frac{-5 \times 4}{6 \times 4} = \frac{-20}{24}$ (ii) $\frac{1}{2}$ Sol. $\frac{1}{2}$
 $\frac{-5}{6} = \frac{-10}{12} = \frac{-15}{18} = \frac{-20}{24}$ (iii) $\frac{1}{2}$ Sol. $\frac{1}{2}$
 $\frac{-5}{6} = \frac{-10}{12} = \frac{-15}{18} = \frac{-20}{24}$ (iv) Compare the following rational numbers by (i) changing them to rational numbers in cquivalent forms (i) using number line:
(iii) $\frac{17}{3} = \frac{17 \times 2}{3 \times 4} = \frac{36}{612}$ (iv) $\frac{2}{3}$ and $\frac{3}{4}$ (iv) $\frac{2}{3}$ and $\frac{3}{4}$ (iv) $\frac{2}{3} = \frac{3}{4}$ (iv) $\frac{3}{4} = \frac{2}{3}$ (iv) $\frac{2}{3} = \frac{3}{4}$ (iv) $\frac{3}{4} = \frac{2}{3}$ (iv) $\frac{3}{4} = \frac{2}{$