

<u>Content</u>

MICROECONOMIC ANALYSIS

Question Paper–June-2023 (Solved)	1-7
Question Paper–December-2022 (Solved)	1-6
Question Paper—Exam Held in March-2022 (Solved)	1-5
Question Paper—Exam Held in August-2021 (Solved)	1-4
Question Paper—Exam Held in February-2021 (Solved)	1-8
Question Paper—June, 2019 (Solved)	1-6
Question Paper—December, 2018 (Solved)	1-5
Question Paper—June, 2018 (Solved)	1-7

S.No.

Chapterwise Reference Book

Page

1.	Theory of Consumer Behaviour : Basic Themes	1
2.	Theory of Demand	9
3.	Theory of Demand : Some Recent Developments	22
4.	Theory of Production	29
5.	Theory of Cost	37
6.	Production Economics	47
7.	Perfect Competition	55
8.	Monopoly	60
9.	Monopolistic Competition	69
10.	Oligopoly	76
11.	Partial and General Equilibrium Approaches : Pure Exchange Model	88

S.No.	Chapterwise Reference Book	Page
12.	General Equilibrium with Production	100
13.	Pigovian Vs. Paretian Approach	110
14.	Social Welfare Function	118
15.	Imperfect Market Externality and Public Goods	127
16.	Social Choice and Welfare	137
17.	Choice in Uncertain Situations	145
18.	Insurance Choice and Risk	
19.	Economics of Information	
20.	Perfect Informative Game	177
21.	Perfect Informative in Active Game – Applications	
22.	Perfect Informative Active Game	
23.	In Active Game with Insufficient Information	
24.	Dynamic Game with Imperfect Information : Pure Bayesian Equilibrium	
25.	Signaling Game and their Applications	214
26.	Modification of Pure Bayesian Equilibrium	219
		-



QUESTION PAPER

June – 2023

(Solved)

MICROECONOMIC ANALYSIS

Time: 3 Hours]

[Maximum Marks: 100

Note: Answer questions from each section as per instructions given.

SECTION-A

Note: Answer any two questions from this Section. Q. 1. (a) An individual consumer's utility function is:

$$\mathbf{U} = q_1 \cdot q_2$$

and her money income is (Y) 100, while the prices are $P_1 = \overline{\xi} 2$ and $P_2 = \overline{\xi} 5$. Find the values of q_1 and q_2 commodities and determine the substitution, income and the price effect.

Ans. To find the values of q_1 and q_2 , we need to maximize the utility function subject to the budget constraint. The consumer's utility function is $U = q_1 \times q_1$ q_2 , and the budget constraint is given by $P_1 \times q_1 + P_2 \times q_2$ = Y, where $P_1 = 2$ and $P_2 = 5$.

The consumer's problem is to maximize utility U subject to the budget constraint:

Maximize $U = q_1 \times q_2$

Subject to $2q_1 + 5q_2 = 100$

To solve this problem, we can use the method of Lagrange multipliers. The Lagrangian for this problem is:

$$L = q_1 \times q_2 - \lambda (2q_1 + 5q_2 - 100)$$

Taking partial derivatives with respect to q_1, q_2 , and λ , and setting them to zero, we can find the values of q_1 , q_2 , and λ .

$$\frac{\partial L}{\partial q_1} = q_2 - 2\lambda = 0 \frac{\partial L}{\partial q_2} = q_1 - 5\lambda = 0 \frac{\partial L}{\partial \lambda} = 2q_1 + 5q_2 - 100 = 0$$

Solving these equations simultaneously will give us the values of q_1, q_2 , and λ .

From the first two equations:

$$\begin{array}{l} q_2 = 2\lambda \\ q_2 = 5\lambda \end{array}$$

Substituting these into the budget constraint equation:

$$2(5\lambda) + 5(2\lambda) = 100$$

$$20\lambda = 100$$

$$\lambda = 5$$

Using $\lambda = 5$, we can find q_1 and q_2 :

$$q_1 = 5(5) = 25$$

$$q_2 = 2(5) = 10$$

So, the consumer will buy 25 units of commodity 1 (q_1) and 10 units of commodity 2 $(2q_2)$ to maximize her utility given the budget constraint.

Now, let's analyze the substitution effect, income effect, and price effect:

Substitution Effect: This refers to the change in the quantity of one good consumed in response to a change in the relative prices of the goods, assuming that the consumer's real income remains constant. In this case, if the relative prices $(P_1 \text{ and } P_2)$ change while real income remains constant, the consumer might adjust the quantities of q_1 and q_2 based on their new relative prices.

Income Effect: This refers to the change in the quantity of goods consumed due to the change in real income. If the consumer's real income changes (i.e., the budget constraint shifts inward or outward), the consumer might change the quantities of both goods consumed.

Price Effect: The price effect combines both the substitution effect and the income effect. It accounts for changes in the quantity of goods consumed due to changes in both relative prices and real income.

(b) Explain the optimum choice of a consumer under the 'Linear Expenditure System'.

Ans. Ref.: See Chapter-3, Page No. 22, 'Recent Development Demand Analysis: Linear Expenditure Systems'.

www.neerajbooks.com

M.E.C.-101

2 / NEERAJ : MICROECONOMIC ANALYSIS (JUNE-2023)

Q. 2. (a) In the context of asymmetric information, how will you find second best solution?

Ans. Ref.: See Chapter-19, Page No. 166, 'Asymmetric Information' and Page No. 175, Q. No. 6.

(b) The vNM utility function of an individual is

 $u = \frac{1}{m^2}$. If her initial wealth is 36, will she accept a

gample in which she wins 13 with a probalility of $\frac{2}{3}$

and lose 11 with probability of $\frac{1}{3}$?

Ans. To determine whether the individual will accept the gamble, we need to compare the expected utility of the gamble with the utility of her initial wealth. The Von Neumann-Morgenstern (vNM) utility function u(m) = m represents her utility function, where *m* is the wealth.

1. Expected Utility from the Gamble: The expected utility EU) from the gamble can be calculated as follows:

EU=
$$(2/3 \times \sqrt{36+13}) + (1/3 \times \sqrt{36-11})$$

EU = $(2/3 \times \sqrt{49}) + (1/3 \times \sqrt{25})$
EU = $(2/3 \times 7) + (1/3 \times 5)$
EU = $38/3$

2. Utility from Initial Wealth: The utility from her initial wealth (u(36)) can be calculated using the vNM utility function:

 $u(36) = \sqrt{36} = 6$ Now, compare the expected utility from the gamble (38/3) with the utility from her initial wealth (6).

38/3>6

Since, the expected utility from the gamble (38/3) is greater than the utility from her initial wealth (6), the individual will accept the gamble. In other words, the potential increase in her expected utility from the gamble is favourable, so she would be willing to take the risk.

(c) Explain Nash equilibrium with an example.

Ans. Ref.: See Chapter-20, Page No. 182, Q. No. 6.

Q. 3. (a) Construct ordinary and compensated demand function for the utility function $U = 2q_1 \cdot q_2 + q_2$. Let the budget constraint be $Y = P_1q_1 + P_2q_2$, where P_1 is the price of good q_1 , P_2 is the price of good q_2 and let consumer's income be given by Y.

Ans. To construct the ordinary and compensated demand functions, we need to maximize the utility function subject to the budget constraint. The utility function is given as $U = 2q_1q_2 + q_2$, and the budget constraint is $Y = P_1q_1 + P_2q_2$, where P_1 and P_2 are the prices of goods q_1 and q_2 respectively.

1. Utility Maximization Problem: The consumer's problem is to maximize the utility function $U = 2q_1q_2 + q_2$ subject to the budget constraint $Y = P_1q_1 + P_2q_2$.

2. Constructing the Lagrangian: To solve this problem, we set up the Lagrangian:

 $L = 2q_1q_2 + q_2 - \lambda(Y - P_1q_1 - P_0q_2)$ Where λ is the Lagrange multiplier.

Partial Derivatives and First-Order Conditions: 1. Partial Derivatives with respect to q_1, q_2 , and λ :

$$\frac{\partial \mathbf{L}}{\partial q_1} = 2q_2 - \lambda \mathbf{P}_1 = 0 \frac{\partial \mathbf{L}}{\partial q_2} = 2q_1 + 1 - \lambda \mathbf{P}_2 = 0 \frac{\partial \mathbf{L}}{\partial \lambda} = \mathbf{Y} - \mathbf{P}_1 q_1 - \mathbf{P}_2 q_2 = 0$$

2. Solving the System of Equations: Solving these equations simultaneously will give us the ordinary demand functions for q_1 and q_2 . Once we have the solutions, we can calculate the compensated demand functions by holding the utility constant.

4. Compensated Demand Functions: To find the compensated demand functions, we assume that the consumer's utility remains constant after a price change. Let's denote the compensated prices as $'P_1'$ and $'P_2'$. The compensated demand functions $('q_1' \text{ and } 'q_2')$ are found by solving the following system of equations:

$$2q_{1}'q_{2}'+q_{2}' = 2q_{1}q_{2}+q_{2}$$
$$q_{1}' + P_{2}'q_{2}' = P_{1}q_{1}+P_{2}q_{2}$$

 $2P_1'q_1' + P_2'q_2' = P_1q_1 + P_2q_2$ Solving these equations simultaneously will give us the compensated demand functions 'q_1' and 'q_2'.

(b) A physician in a small village charges higher price for check-up to rich patients whereas lower prices to poor patients. Why does she charge different prices?

Ans. Ref.: See Chapter-8, Page No. 67, Q. No. 9.

(c) Prove diagrammatically that a monopolistic firm charges a higher price than a competitive firm.

Ans. To demonstrate graphically why a monopolistic firm charges a higher price than a competitive firm, we can compare the market structures in terms of their demand and marginal revenue curves. Let's draw the graphs for both monopolistic and competitive firms and analyze their pricing decisions.

Monopolistic Firm: In a monopolistic market, a single firm has control over the entire market. It faces a downward-sloping demand curve (D) because it's the



MICROECONOMIC ANALYSIS

Theory of Consumer Behaviour : Basic Themes

INTRODUCTION

Market aggregate demand curve for a commodity is downward sloping in a situation where market prices are given to consumers and they cannot influence the market prices by changing their consumption. Here, we will investigate the economic rationality behind this for a commodity of all individual consumers. This chapter will enable you to determine the optimum choice of a consumer, explain how the price effect can be decomposed into income effect and substitution effect and determine the individual demand curve. The market demand mainly depends on the nature of demand for a commodity by individual consumers and the demand for a commodity of an individual consumer depends upon the behaviour of the consumer. Now we will begin with the analysis of consumer behaviour to clearly investigate the economic rationality behind the law of demand.

CHAPTER AT A GLANCE

THE BASIC THEMES

The consumer behaviour can be analysed through different approaches. In all approaches, it is assumed that the consumer is rational and derives maximum utility from a given amount of money. He compares the marginal utility derived from one commodity bundle with the marginal utility derived from another commodity bundle and chooses one commodity bundle from among all the commodity bundles. The consumer distributes the resources which are with him in such a way that he derives maximum satisfaction.

The assumption will be based on the condition that the consumer has a fixed income and the prices of all goods are given and are fully known to the consumer. **CONSUMER CHOICE CONCERNING UTILITY**

Every commodity which a consumer consumes yields some utility and the utility is a measurable

concept. The consumer cannot maximize his satisfaction unless he measures utility of a commodity. Utility can be measured differently by different approaches. However, there are two main approaches:

- 1. Cardinal Theory : An Introduction
- 2. Ordinal Theory : A Short Note

1. Cardinal Theory: An Introduction

The cardinal utility approach is also known as marginal utility analysis. In this approach, utility derived from each commodity is measured on a cardinal scale or numerically in terms of money. It is a short period analysis and here the consumer knows which commodity is preferred and the price of that commodity.

Following are the main assumptions of the cardinal utility approach.

- 1. Consumer is rational. He aims at maximizing his utility by selecting one of the commodity bundles at given prices of commodities and money income.
- **2.** The total utility of the consumer depends on the quantity of consumption, if the taste and preferences are given.
- **3.** Goods are good. The marginal utility is positive. It means if 'U' is utility level of the consumer and 'x' the consumption level, as 'x' increases (decreases), 'U' increases (decreases).
- **4.** Marginal utility of 'x' is diminishing or downward sloping. It means a 'x' increases (decreases), the MU_x (marginal utility of the consumption) decreases (increases).
- 5. Utility is measured cardinally or numerically in terms of money. Therefore, the consumer knows which commodity bundle is preferred and by how much amount.
- 6. The Marginal Utility of money (MU_m) is positive and constant. The validity of this assumption is that the money is used as a measuring rod of utility. Thus $MU_m = \lambda$, where λ is positive and constant. It means as money income increases (decreases) by one unit, utility increases (decreases) by λ unit.

2 / NEERAJ : MICROECONOMIC ANALYSIS

Consumer Equilibrium

As per the assumption, the gross unity the consumer gets is U(q) for 'q' unit of consumption of the commodity. Here, the consumer must spend p_q . q units of money income if p_q is the cost of the commodity 'q', which is given to the consumer. Thus, the net utility (N(q)) of the consumer will be N(q) = U(q) - λp_q . q, where λ and p_q are provided to the consumer and λ represents fall in utility due to one unit fall in money income.

The consumer's objective is to maximize net utility N(q) by choosing 'q'. For that, we can take the first

derivative of N(q) and set that equal to zero, $\frac{dN(q)}{dq}$

= 0. Or, consumer equilibrium, we get $\frac{dU(q)}{dq} - \lambda p_q$

= 0. From the first order condition, we can derive the maximum value of 'q' which is (say) $q^* = q^* (p_q, \lambda)$. The second order condition for utility optimization needs

 $\frac{\partial^2 N(q)}{\partial q^2} = \frac{\partial^2 U(q)}{\partial q^2} < 0, \text{ which is ensured by the assumption of falling MU}_{q}.$



2. Ordinal Theory: A Short Note

In ordinal method, utility of a commodity is measured ordinarily or qualitatively and not quantitatively or numerically. Here, the consumer can rank his preferences alternatively as per the order he wants to compare but not in terms of different amounts. Thus, it is more realistic measurement of utility. There are two types of approaches to measure utility in ordinal theory:

1. Indifferent Curve Approach

2. Revealed Preference Approach.

1. Indifferent Curve Approach: Indifference curve is made by taking utility level constant. Thus, different indifferent curves denote different level of utility for some consumers. The equilibrium is obtained when indifferent curve become tangent to the budget line or price line.

2. Revealed Preference Approach: In this approach, consumer equilibrium is obtained by ranking different bundle of goods in the commodity space. The consumer picks the best bundle for which his utility will optimize. Famous economist Paul A Samuelson is the founder of this method.

INTRODUCTION TO DEMAND ANALYSIS

Market demand curve or aggregate individual demand curves, is generally downward sloping. Individual demand curve is made by combining different consumer equilibrium for different prices. Here, the market price is fixed and given to the consumer. In neo-classical theory, demand curve can be obtained if the price is changed exogenously and join all the equilibrium points. In the following section, we will find the individual demand curve by using ordinal theory and taking indifferent curve approach. **ORDINAL THEORY:**

INDIFFERENCE CURVEAPPROACH

In indifference curve approach, the objective of consumer is to maximize his utility by choosing a bundle of commodities among all other available commodity bundles (under budget constraint) where total utility depends on quantity of consumption given his taste and preferences. In a two-commodity world, (if we take x_1 and x_2) utility function is given by $U = U(x_1, x_2)$ and it depends on the consumer's taste and preferences, which is specified by the following axioms:

1. Axiom of Reflexiveness: Consumer's choice is reflexiveness.

If there are two commodities x_1 and x_2 and x_1 is weakly preferred to x_2 , we can say $x_2 Rx_1$ (R stands for weak preference relation). It implies that either x_1 is strictly preferred over $x_2 (x_1 Px_2)$ or x_1 is indifference to $x_2 (x_1 Ix_2)$. Here, P and I stand for strict preference relation and indifference respectively.

Any commodity bundle is either strictly preferred or indifferent over any other commodity bundle. Consumer can choose any commodity bundle. So choice set of this specified by the commodity set 'X'.

2. Axiom of Completeness: Consumer choice is complete.

Consumer, being a rational, must have a unique preference relation. It means the consumer choice will be either x_2Rx_1 or x_1Rx_2 . Consumer choice is also consistent or comparable. Consumer choice must be transitive because of unique preference relations. Thus, it can be x_1Rx_2 , x_2Rx_3 or x_1Rx_3 . x_3 is another commodity.

3. Axiom of Continuity: Consumer's preference relation (R) is continuous. Consumer looks for better one continuously, comparing one with the other commodity. Thus, it is a continuous process. Following three axioms can be included under this:

(a) Axiom of Non-satiation: Consumer's choice is non-satiated in all goods.

It implies that larger the consumption of a commodity leads to larger satisfaction or utility and lower the consumption lower is the satisfaction or

THEORY OF CONSUMER BEHAVIOUR : BASIC THEMES / 3

utility. It also denotes that "goods are good" and "more is better". Thus, A will be preferred over B (APB) if A has larger quantity than $B(A \ge B)$.

- (b) Axiom of Convexity: The indifference curve for consumer choice is strictly convex to the origin. So the utility is quasi-concave.
- (c) Axiom of Selfishness: Consumer choice is selfish. Consumer choice is self-guarded and it is not influenced by any other consumer.

Concept of Preference, Utility Function and Indifference Curve

As specified by the above axioms, consumer preference ('R') can be represented by a function where total utility ('U') depends upon the quantity consumption (x_1, x_2) which satisfied all other axioms. Utility function is $U(x_1, x_2)$ which is otherwise U, which the consumer aims to optimize.

Meaning and Definition of Indifference Curve: Indifference curve is a graphical tool to solve the consumer utility maximization problem. Indifference curve is constructed in commodity - commodity plane by joining different goods along which the consumer is indifferent (or he has same level of utility). Therefore, along the indifference curve utility or satisfaction remains unchanged.

Existence of Indifference Curve: Indifferent curve may exit anywhere in the commodity space. It is because consumer may be indifferent between any commodity bundles and such as choice might be continuous. Also, because of axiom of reflexiveness consumer can choose a commodity bundle over another commodity bundle and such a choice might be continuous.

Derivation of Indifference Curve and its Properties Graphical Presentation

In the diagram given below, there are good I (x^0_1) and Good II (x^0_2) , from which the consumer gets some utility (U_0) . Here, we compare the two commodity bundles and for which we divide the commodity plane into four phases.





any point in 'b' in vertical axis, we have larger x_2 with same x_1 . It means in Phase I, including the borderlines, there is large quantity of at least one good and no less quantity of any other good compared to 'A'. Thus, we have larger utility in Phase I including the borderlines compared to 'A'.

By similar logic, we have lower consumption of at least one good and no large consumption of any other good in Phase III including the borderlines compared to point 'A'. Hence, there is lower level of utility in Phase III including the borderlines compared to 'A' by the axiom of non-satiation for all commodities.

It is clear that utility is not constant between the good bundles compared to point 'A' in phases I and III, including borderlines. Therefore, indifference curve (along which utility is constant) cannot pass through phases I and III including their borderlines.

Take any point in phase IV, excluding borderlines (α), we have larger x_1 (for which utility is larger) and lower x_2 (for which utility is lower) compared to 'A'. Since both the goods are non-satiated, utility of point α may be larger, lower or equal compared to point 'A'. In the same way, for any point in phase II, excluding the borderlines (δ), there is larger consumption of x_2 but lower of x_1 compared to point 'A'. So, by axiom of nonsatiation in all goods, utility at point δ may be larger, lower or equal compared to point 'A'.

It is clear that only in Phases II and IV, excluding the borderlines, there is a possibility of the same level of utility between the bundles compared to point 'A'. So indifference curve, along which utility remains constant, must pass through Phases II and IV, excluding their borderlines. Hence, indifference curve is necessarily downward sloping where all goods are non-satiated given that a consumer choice is reflexive, continuous and complete.

Mathematical Presentation

If the utility function is $U = U(x_1, x_2)$, by differentiating we get:

$$dU = U_1 dx_1 + U_2 dx_2 = 0$$
 (as along the indifference
 dx_2

curve utility is unchanged, dU = 0). So $\frac{1}{dx_1}$

$$U_1(x_1, x_2)$$

 $=\frac{1}{U_2(x_1,x_2)}$ = is the slope of the indifference curve. It

is negative since $U_1(x_1, x_2) > 0$ and $U_2(x_1, x_2) > 0$ by axiom of non-satiation of all commodities. Therefore, indifference curve is downward sloping as all goods are non-satiated and choice is continuous, reflexive and complete.

Economic Meaning

All goods are non-satiated that means larger (lower) assumption leads to larger (lower) utility. So, for given x_2 , as x_1 increases, utility rises. Hence, to maintain the same level, utility must be reduced, which is possible

4 / NEERAJ : MICROECONOMIC ANALYSIS

by cutting x_2 . So, as x_1 increases, x_2 must falls to maintain the same level of satisfaction. Because of that indifference curve is downward sloping.

Properties of Indifference Curve

Property I: Higher indifference curve gives higher utility.



Explanation: Since all goods are non-satiated, larger consumption of any good leads to larger utility. Hence, a commodity bundle, which has larger quantity of atleast one good and no less consumption of any other goods, provides larger utility compared to any other commodity bundles. In results, higher indifference curve stands for higher consumption of at least one good and no less consumption of any other goods.

Property II: Indifference curves cannot intersect with each other.



Explanation: Suppose two indifference curves intersect each other. By definition, utility is unchanged along the indifference curve, Thus, consumer is indifferent between points 'A' and 'C' that lie on the same indifference curve. Similarly, consumer is indifferent between points 'B' and 'C', as they also lie on the same indifference curve. So AIC and BIC, where 'I' implies indifference. Now, from transitivity there is AIB, that

means point 'A' and 'B' give the same utility to the consumer. But for given x_2 , x_1 is larger in point 'A' compared to point 'B'. So, by the assumption of non-satiation, we have point 'A' that provides larger utility to consumer as compared to point 'B'. This is a contradiction on the fact that point 'A' and 'B' gives the same level of utility to the consumer (as we have proved above). Thus, when all goods are non-satiated and transitivity holds, indifference curves cannot intersect. **Utility Maximization**

Graphical Presentation: Suppose there are two commodity world, x_1 and x_2 representing commodity I and II respectively. Prices, given to the consumer, of good I and II are p_1 and p_2 respectively. Prices here are exogenously given and consumer cannot change them. The consumer's money income (M) is also exogenously given to the consumer. Note that $p_1x_1 + p_2x_2$ is the total expenditure of the consumer when he consumes x_1 units of good I and x_2 units good II. The total expenditure of the consumer cannot exceed his money income, thus

 $p_1x_1 + p_2x_2 \le M$...(*a*) Equation (*a*) is the consumer's budget constraint. Let $U = U(x_1, x_2)$ is the utility function of the consumer. So, consumer must solve the following optimization problem (UMP):

Problem UMP: Max U (x_1, x_2) Subject to $x_1 > 0$ $x_2 > 0$ and $p_1x_1 + p_2x_2 \le M$



As consumer aims to optimize his utility and as longer consumption results in larger utility, he always wants to have more of any goods. But he also has to spend some amount of his income to consume larger amount of goods. So, ultimately in equilibrium he will spend all her income and $M = p_1x_1 + p_2x_2$.

Now if the line segment AB stands for the price line or budget line. Along AB $p_1x_1 + p_2 x_2 = M$ holds. Suppose, initial indifference curve of the consumer is IC₀. In IC₀, there are many points along that indifference curve such that $p_1x_1 + p_2 x_2 \le M$ holds. Thus, utility optimizing consumer will spend more as he moves to